

PIC Simulations of Sunward and Anti-sunward Whistler Waves in the Solar Wind

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Heat flux in the solar wind

The collisional Spitzer-Härm law is not applicable in the solar wind and solar corona [e.g., Hollweg 1974; Scudder, 1992]

The heat flux suppression below the collisional values was demonstrated by direct in-situ measurements in the solar wind (Feldman+ JGR 1975; Scime+ JGR, 1994; Gary+ Phys. Plasmas 1999; Tong+ ApJ 2019)

One of the possible mechanisms of the heat flux regulation in the solar wind is the wave-particle interaction. It was hypothesized that whistler waves driven by the whistler heat flux instability might be responsible for the heat flux regulation (Gary+ Phys. Plasmas, 1999; ApJ 2000)

$$q_e \sim \int (\mathbf{v} - \langle \mathbf{v} \rangle) (\mathbf{v} - \langle \mathbf{v} \rangle)^2 f(\mathbf{v}) d^3v$$

$$\langle \mathbf{v} \rangle = \int \mathbf{v} f(\mathbf{v}) d^3v$$

Spitzer-Härm law

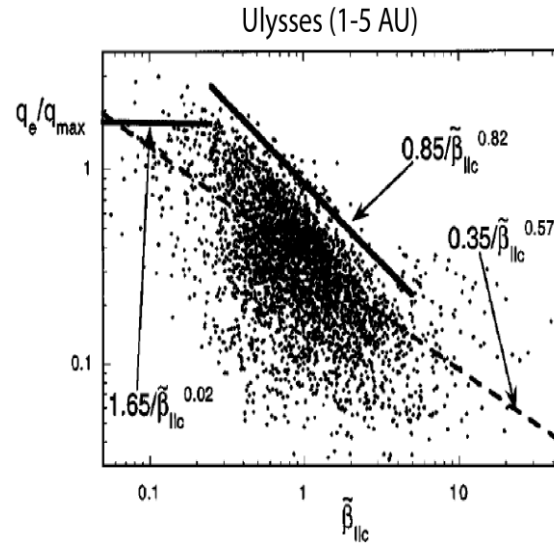
$$q_e = -\kappa \nabla T_e$$

there is an upper bound on the electron heat flux that depends on the electron beta

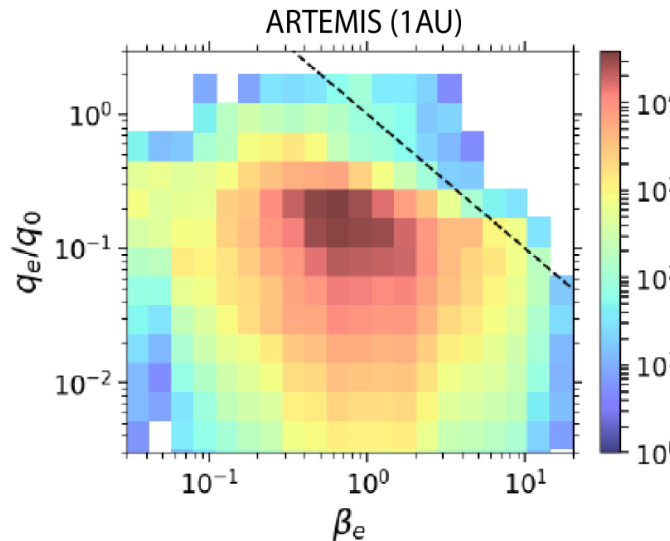
$$q_e/q_0 \lesssim A \beta_e^{-\alpha}$$

$$\beta_e = 8\pi n_e T_e / B_0^2$$

$$q_0 = 1.5 n_e T_e (2T_e/m_e)^{1/2}$$

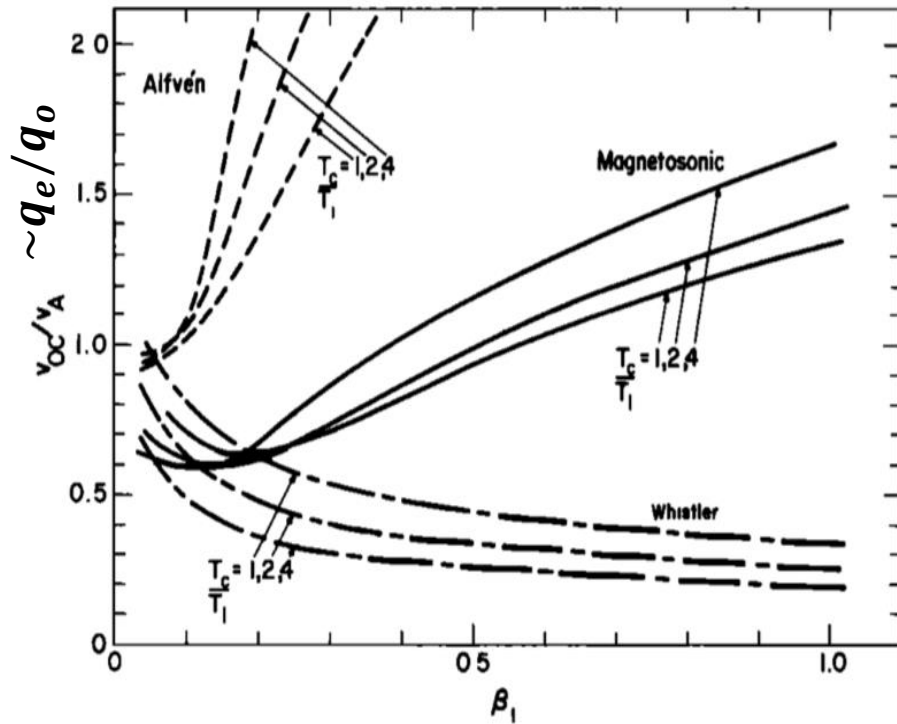


Gary+ Phys. Plasmas 1999

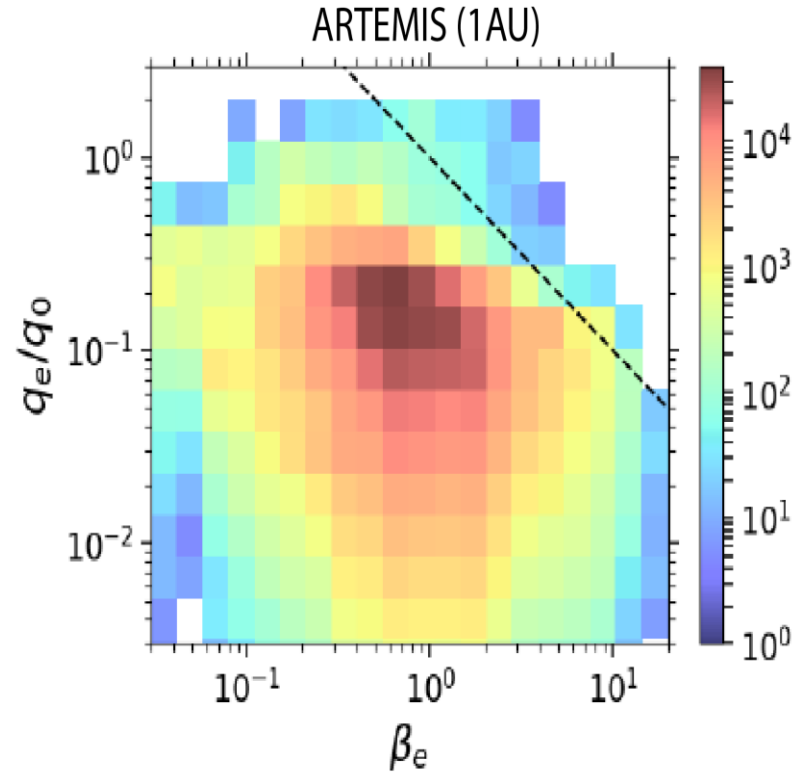


Tong+ ApJ 2019

Heat flux regulation in the solar wind



Gary+ JGR 1975



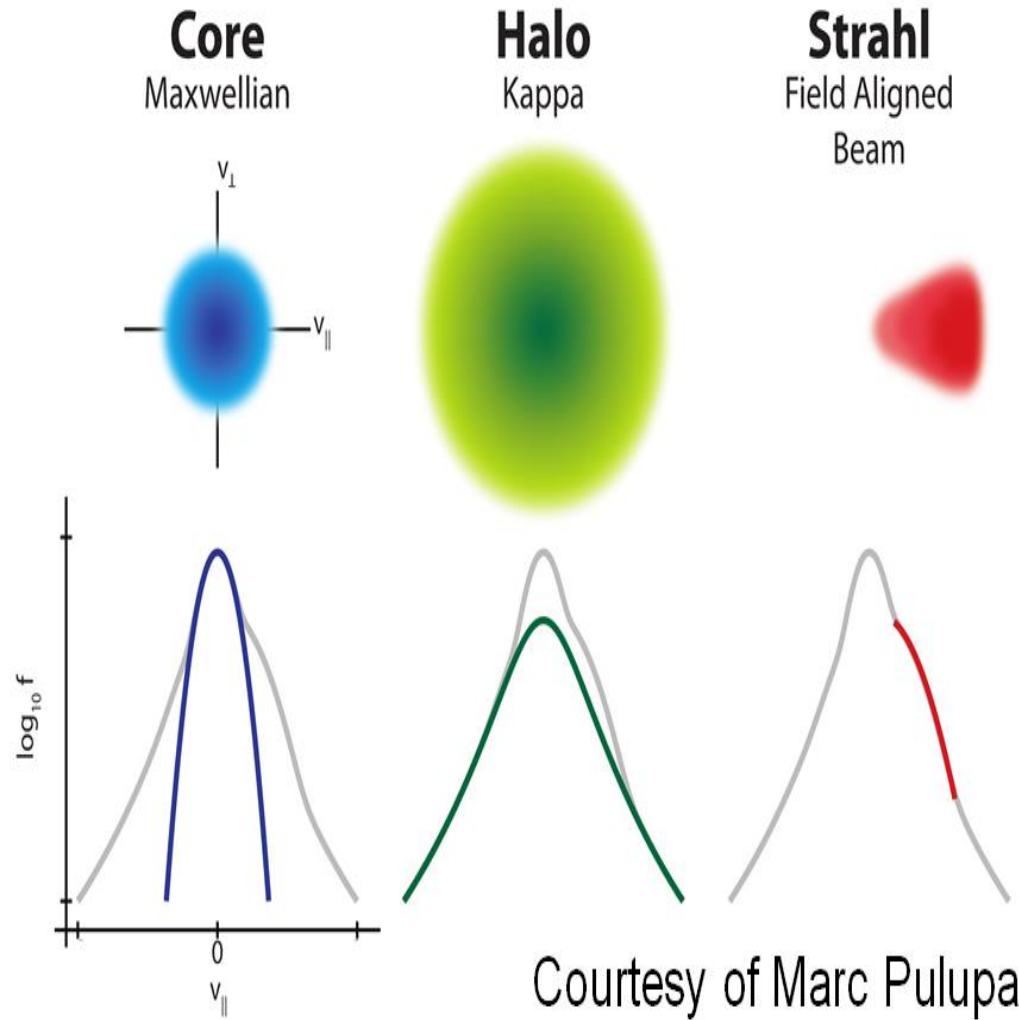
Tong+ APJ 2019

the major argument behind Gary+ hypothesis:
 beta dependence of the observed upper bound on the electron heat flux is
 similar to the linear marginal stability threshold of the WHFI

Whistler waves: R-mode with frequencies

$$\omega_{ci} \ll \omega < \omega_{ce}$$

Solar wind electrons



- three electron populations drift along magnetic field lines
- halo and strahl electrons carry the major part of the electron heat flux that is generally directed anti-sunward
- core electrons drift sunward to keep zero current

Whistler instabilities

electrons = Maxwellian Core + Maxwellian Halo:

$$F_e = \frac{n_c}{(2\pi v_c^2)^{3/2}} \exp\left(-\frac{(\vec{v} - \vec{u}_c)^2}{2v_c^2}\right) + \frac{n_h}{(2\pi v_h^2)^{3/2} A_h} \exp\left(-\frac{(v_{\parallel} - u_h)^2}{2v_h^2} - \frac{v_{\perp}^2}{2v_h^2 A_h}\right)$$

$$A_h = \frac{T_{h\perp}}{T_{h\parallel}}; \quad v_{c,h} = \sqrt{\frac{T_{c,h\parallel}}{m_e}}$$

WHFI: Whistler Heat Flux Instability

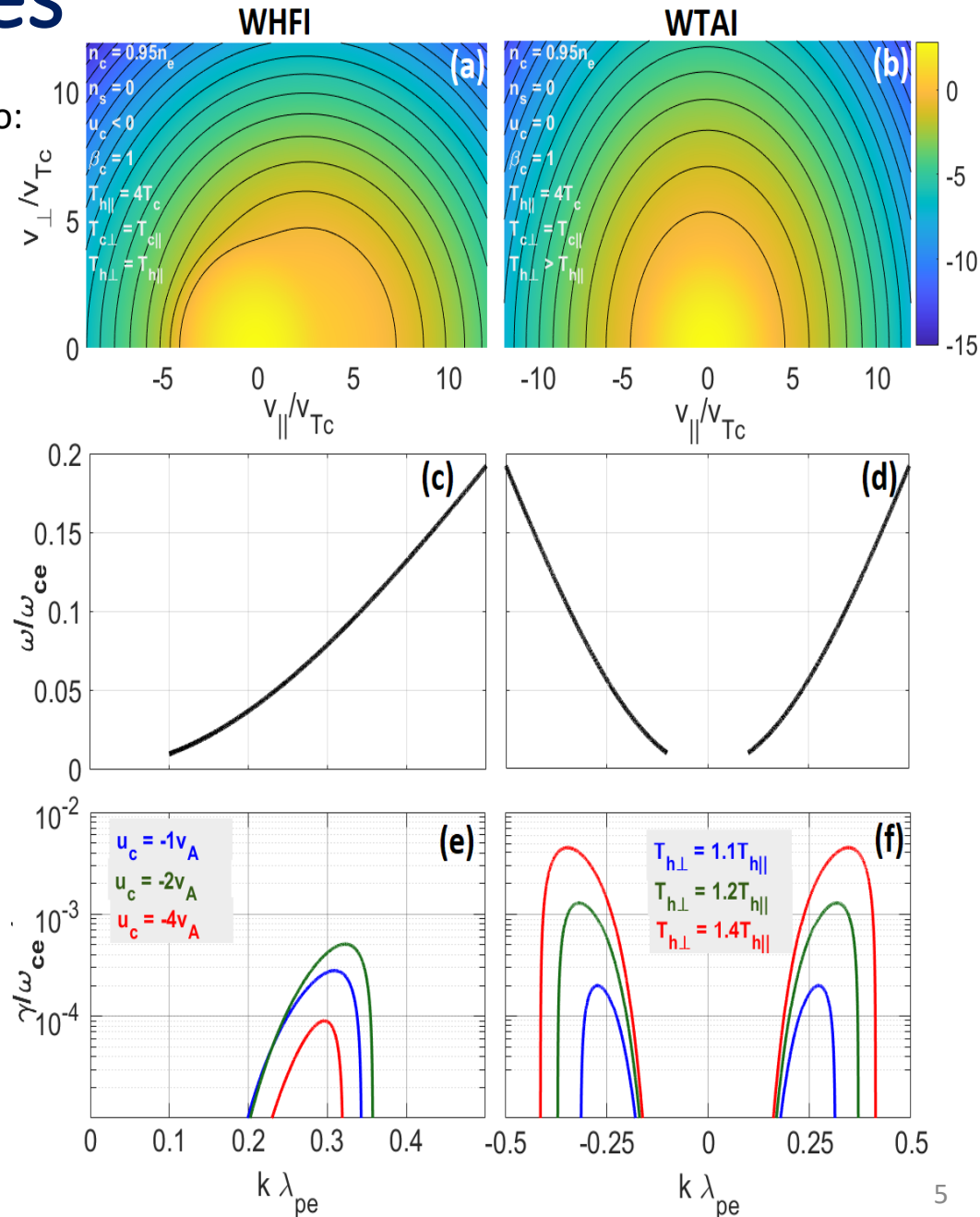
Generates only parallel whistler waves

Does not reduce the heat flux

(Kuzichev et al. ApJ 2019)

WTAI: Whistler Temperature Anisotropy Instability

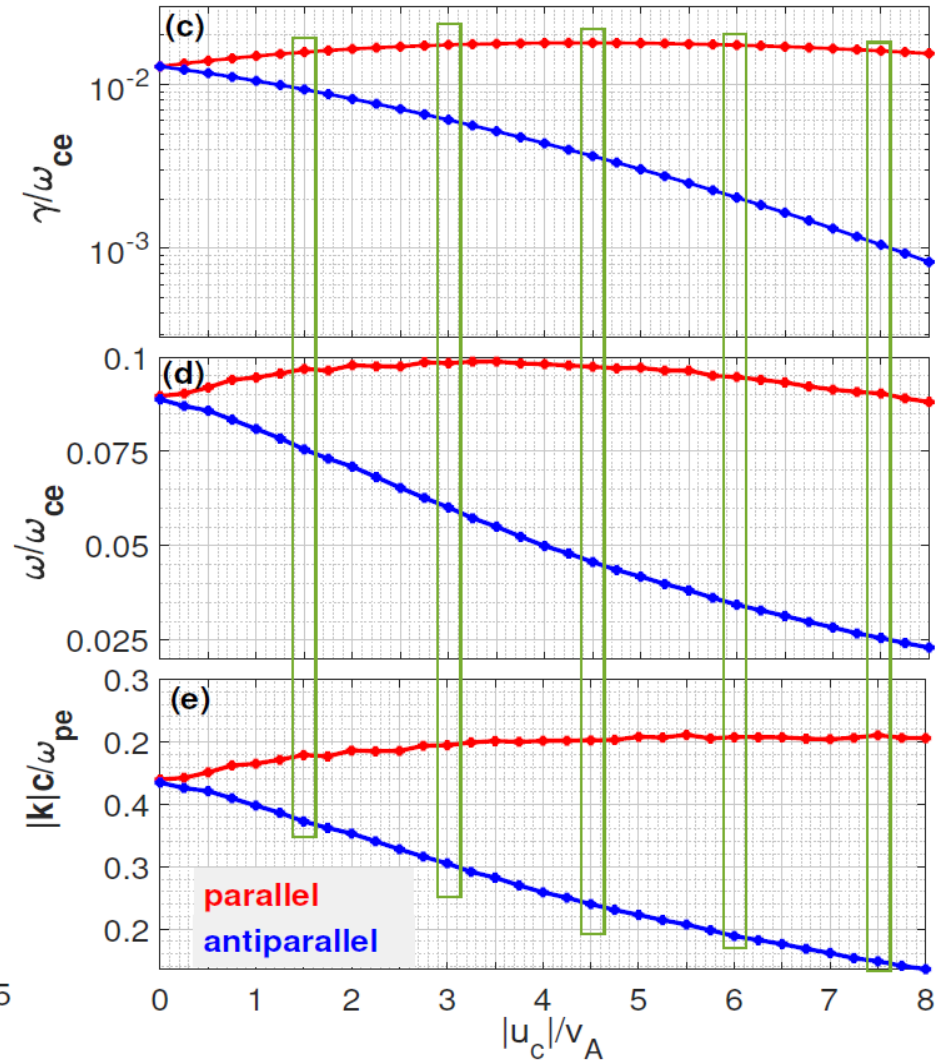
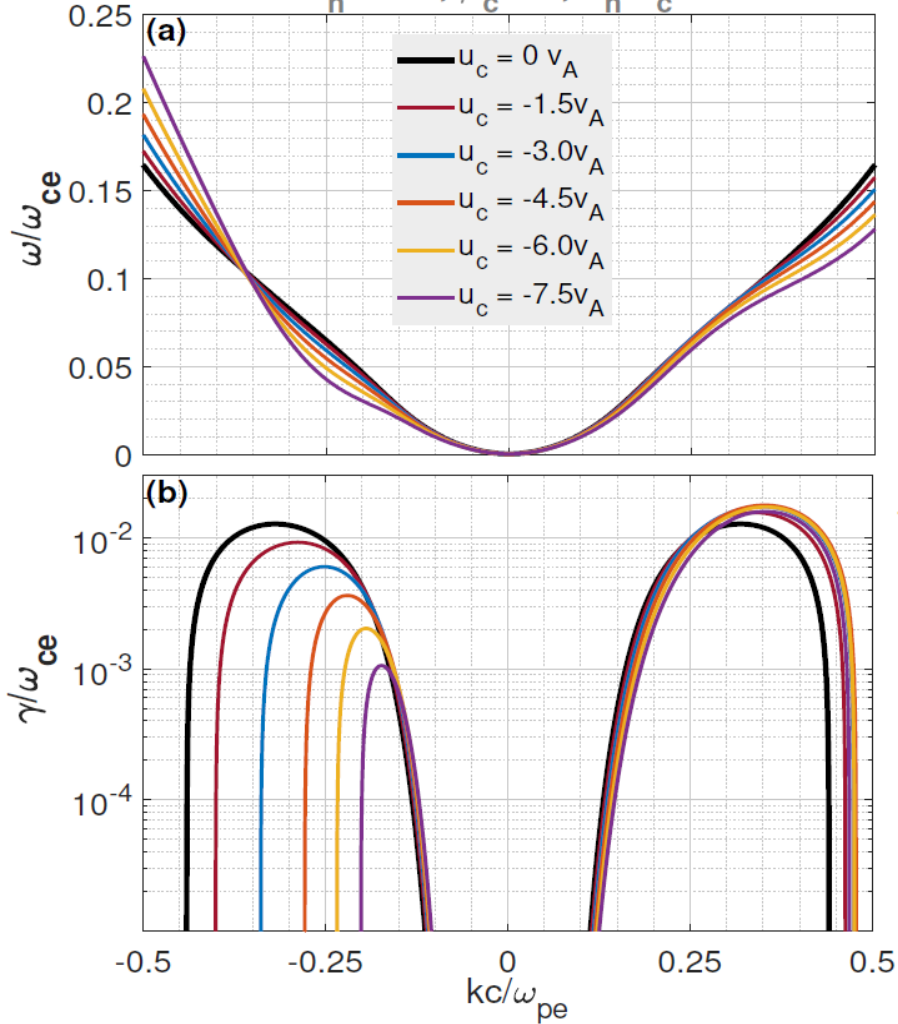
Generates both parallel and anti-parallel whistler waves



Effects of anisotropy on WHFI: linear theory

$$F_e = \frac{n_c}{(2\pi v_c^2)^{3/2}} \exp\left(-\frac{(\vec{v} - \vec{u}_c)^2}{2v_c^2}\right) + \frac{n_h}{(2\pi v_h^2)^{3/2} A_h} \exp\left(-\frac{(v_{\parallel} - u_h)^2}{2v_h^2} - \frac{v_{\perp}^2}{2v_h^2 A_h}\right) \quad A_h = \frac{T_{h\perp}}{T_{h\parallel}}; v_{c,h} = \sqrt{\frac{T_{c,h\parallel}}{m_e}}$$

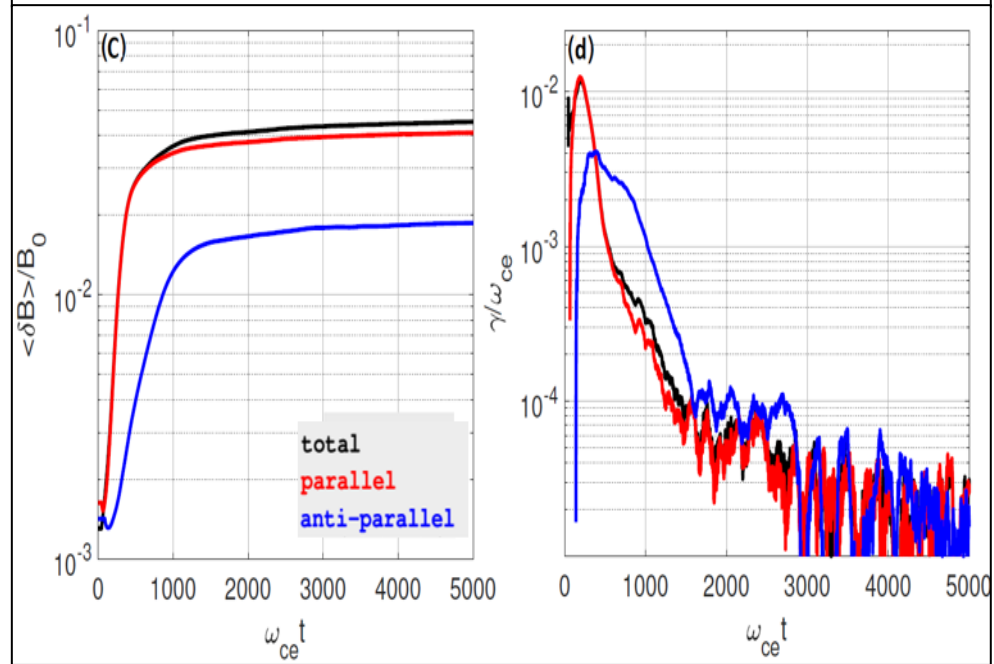
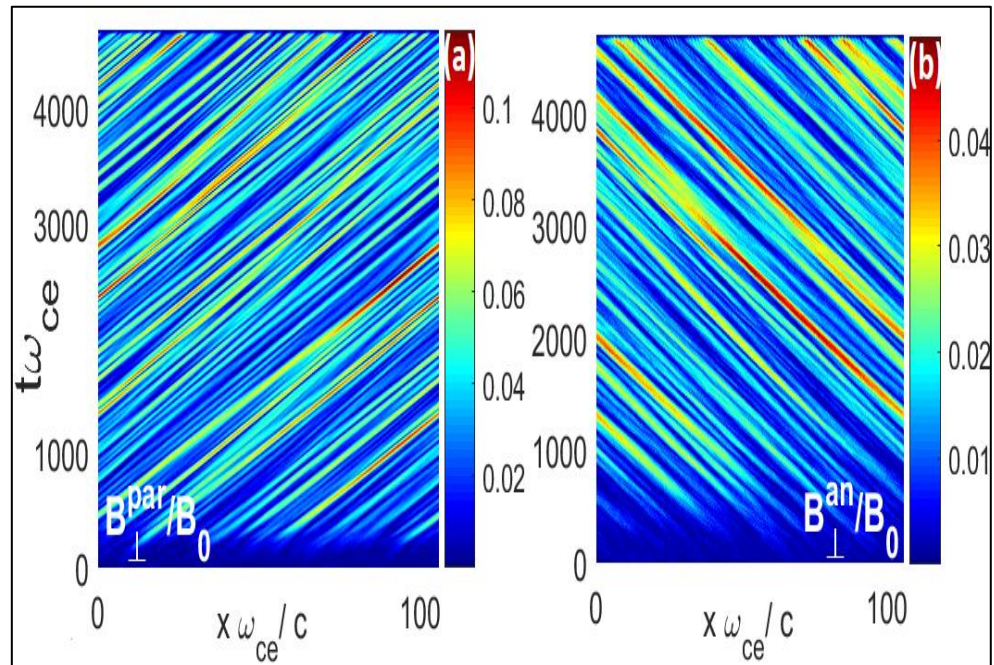
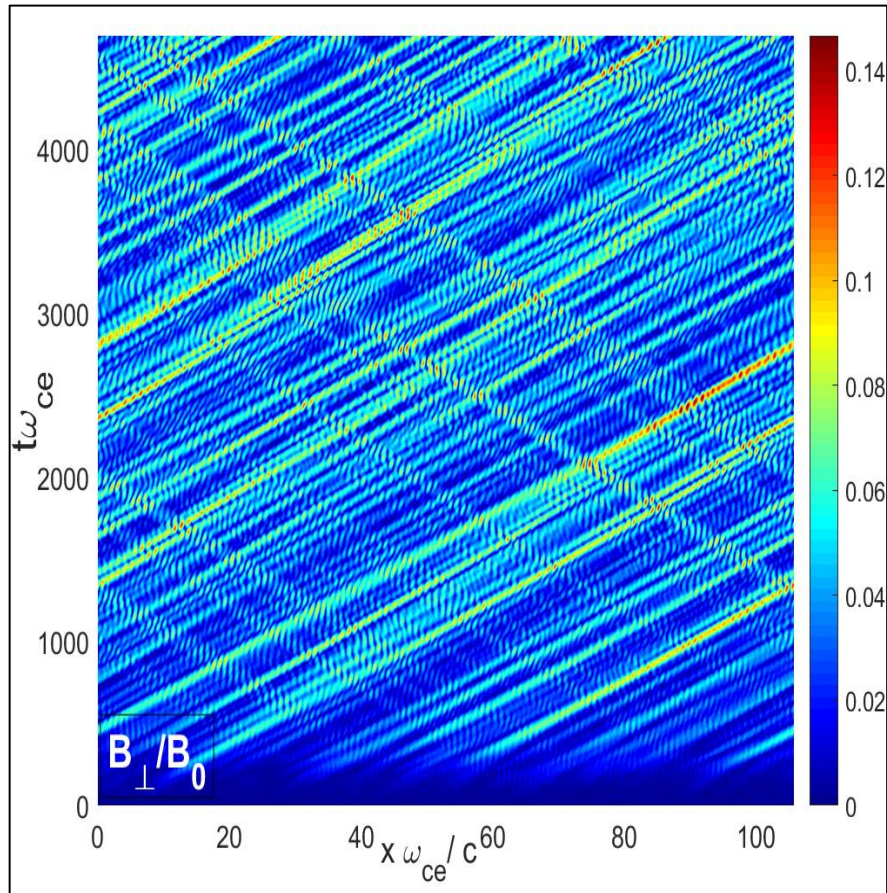
$A_h = 1.3, \beta_c = 1, T_h/T_c = 6$



PIC simulations

$$\beta_c = 1, n_c = 0.85, u_c = -3v_A$$

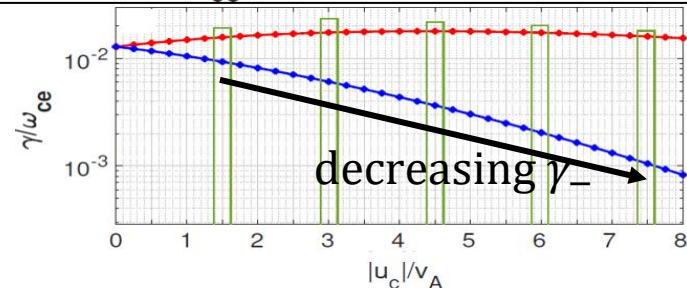
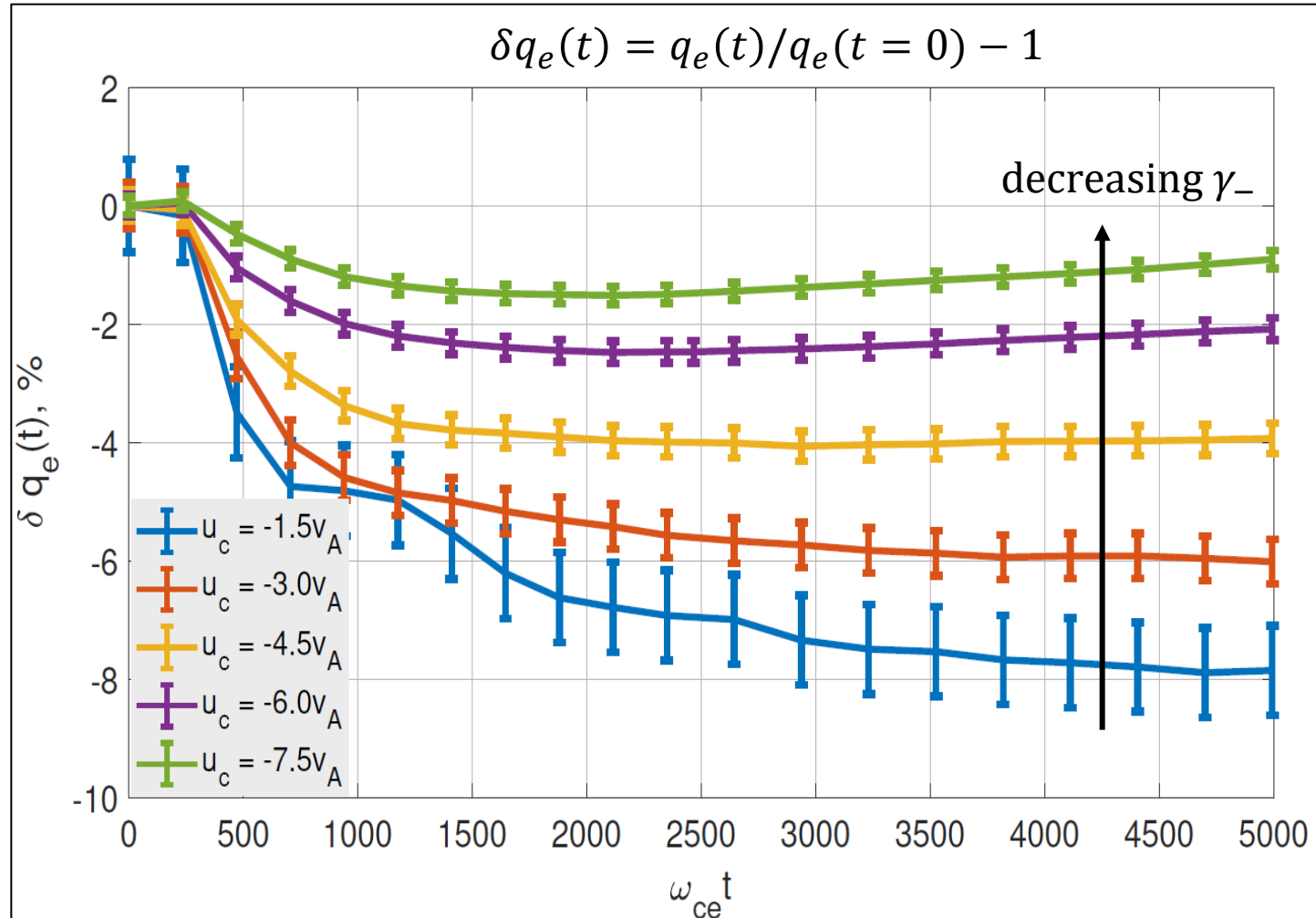
$$A_h = 1.3, v_h^2/v_c^2 = 6$$



$$\langle \delta B(t) \rangle = \sqrt{\langle B_{\perp}^2(t, x) \rangle_x}$$

Heat flux variation for $A_h = 1.3, \beta_c = 1$

- Heat flux decreases by up to 10%
- Heat flux variation is correlated with the linear growth rate for the anti-parallel whistler waves.
- Growth rates (and, consequently, saturated amplitudes) of the parallel whistlers are almost the same for all of the simulations.

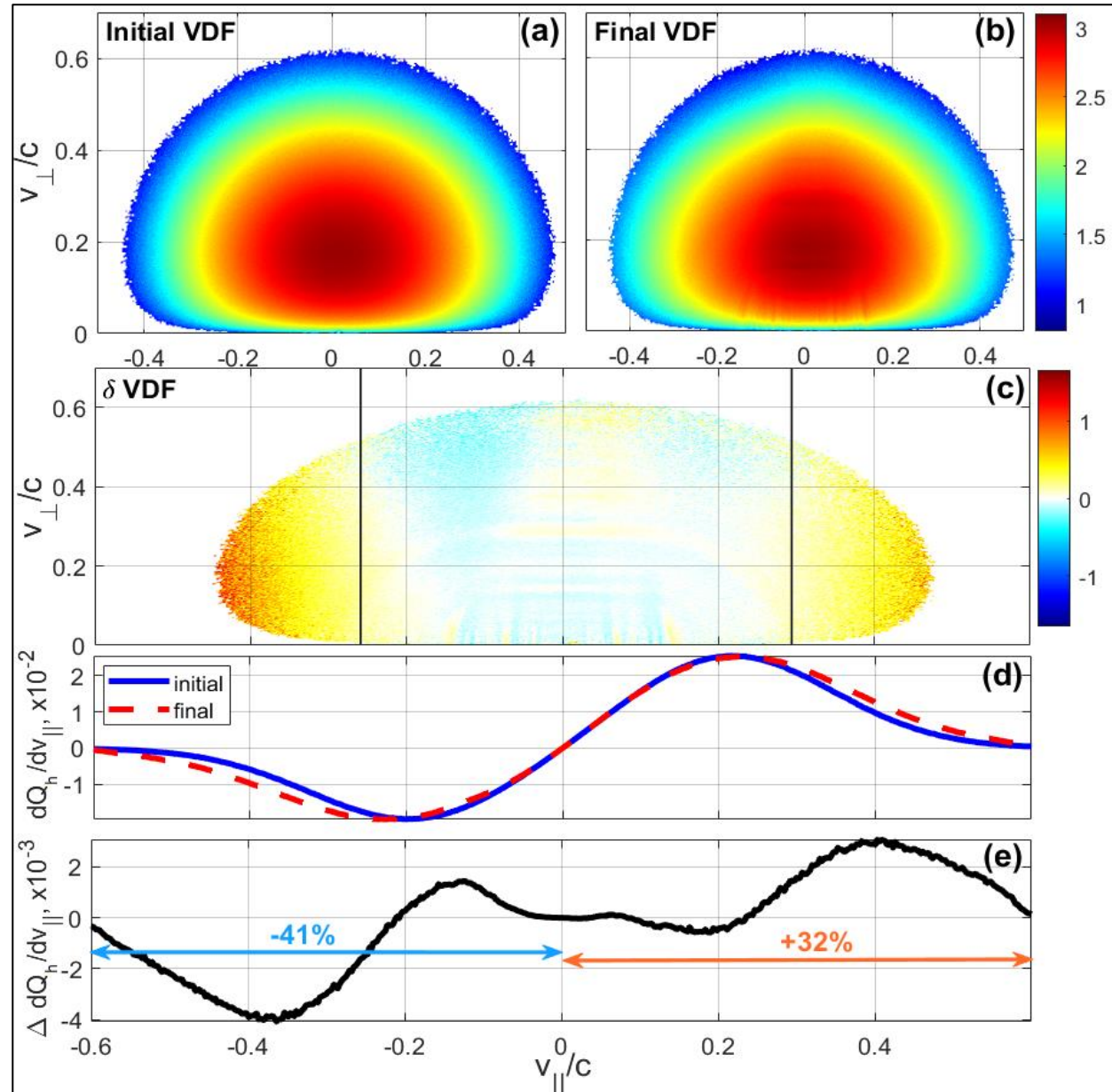


What changes the heat flux?

- Variation of the phase space density (for hot electrons) demonstrate that the instability saturation is consistent with the QL theory predictions: formation of a plateau around the resonant velocities (black vertical lines)
- Parallel heat flux density shows

$$\frac{dQ_h}{dv_{\parallel}} = \frac{m_e}{2} \int v_{\parallel} \mathbf{v}^2 f_h(\mathbf{v}) d^2 v_{\perp}$$

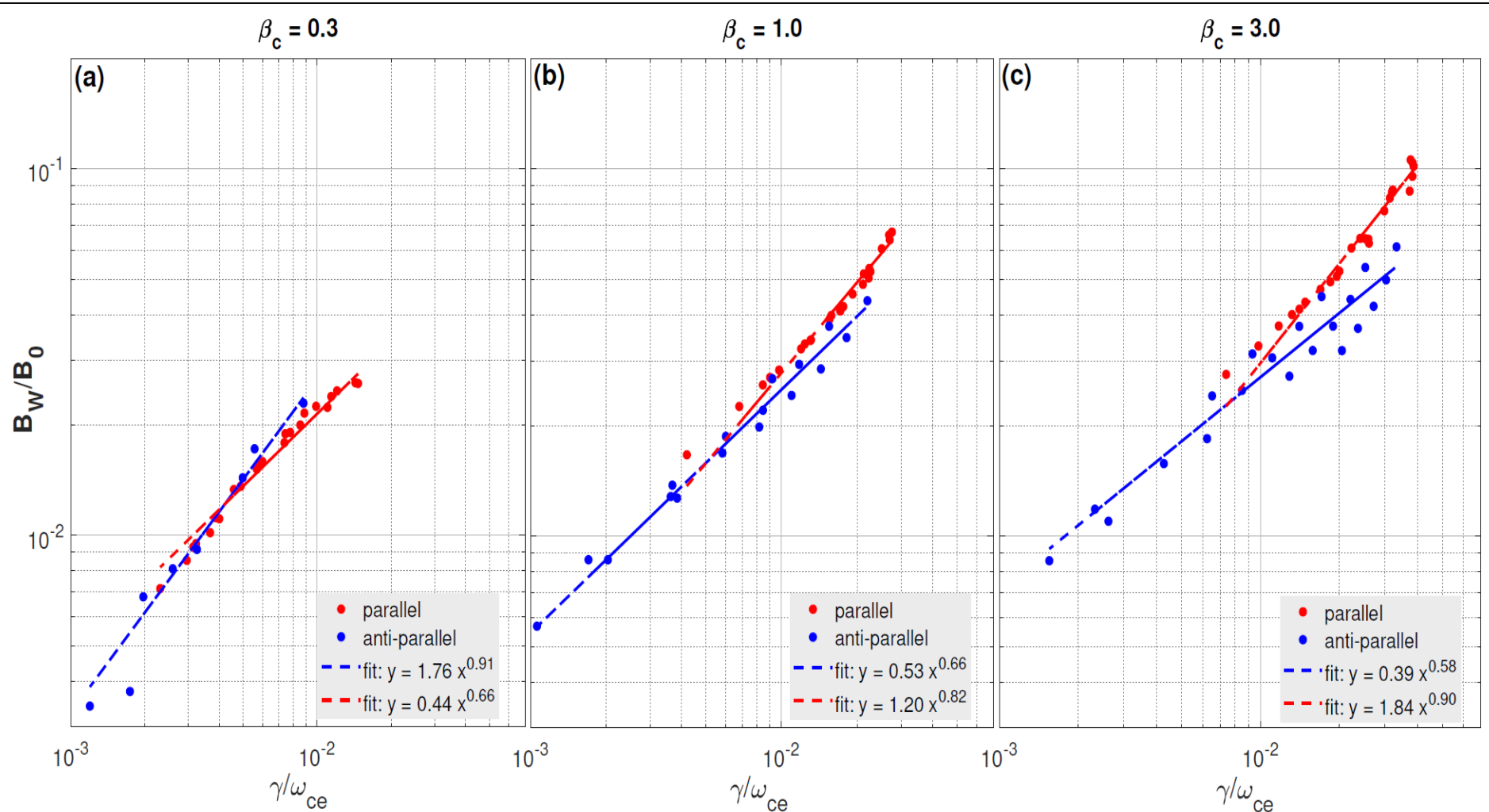
that the anti-parallel waves increase the heat flux, while the parallel waves decrease it, with overall effect being a heat flux reduction.



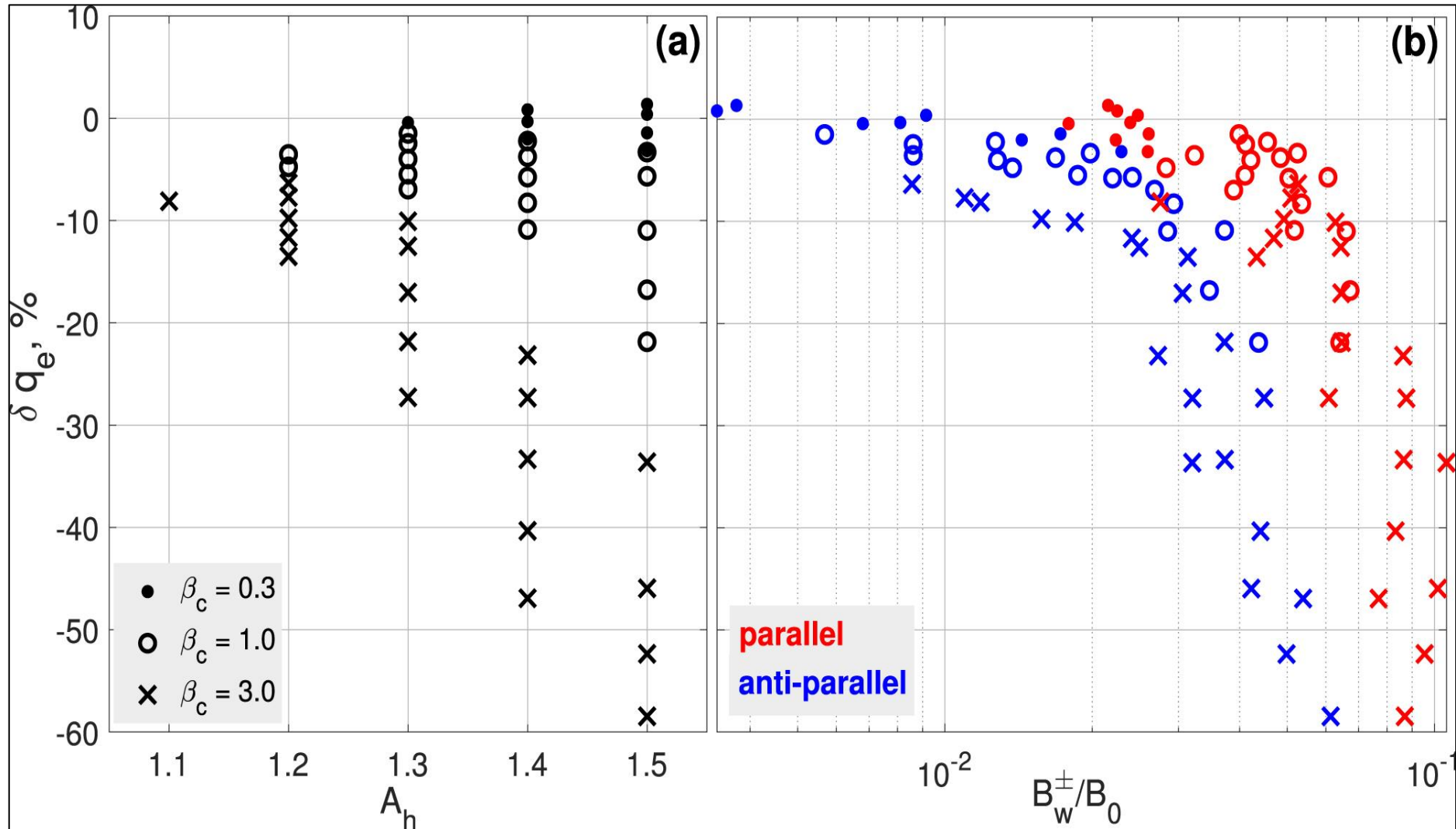
Full set of simulations: scalings

run sets	β_c	$-u_c/v_A$	A_h
I	0.3	1.5:1.5:7.5	1.1:0.1:1.5
II	1	1.5:1.5:7.5	1.1:0.1:1.5
III	3	1.5:1.5:7.5	1.1:0.1:1.5

$$B_w^\pm/B_0 = C_\pm (\gamma_\pm/\omega_{ce})^{\nu_\pm} \quad \nu_\pm \in (0.6, 0.9)$$



Full set of simulations: heat flux variation



Full set of simulations: wave frequencies

$$\omega = \frac{\int PSD(\omega') \omega' d\omega'}{\int PSD(\omega') d\omega'}$$

$$\Delta\omega^2 = \frac{\int PSD(\omega') (\omega' - \omega)^2 d\omega'}{\int PSD(\omega') d\omega'}$$

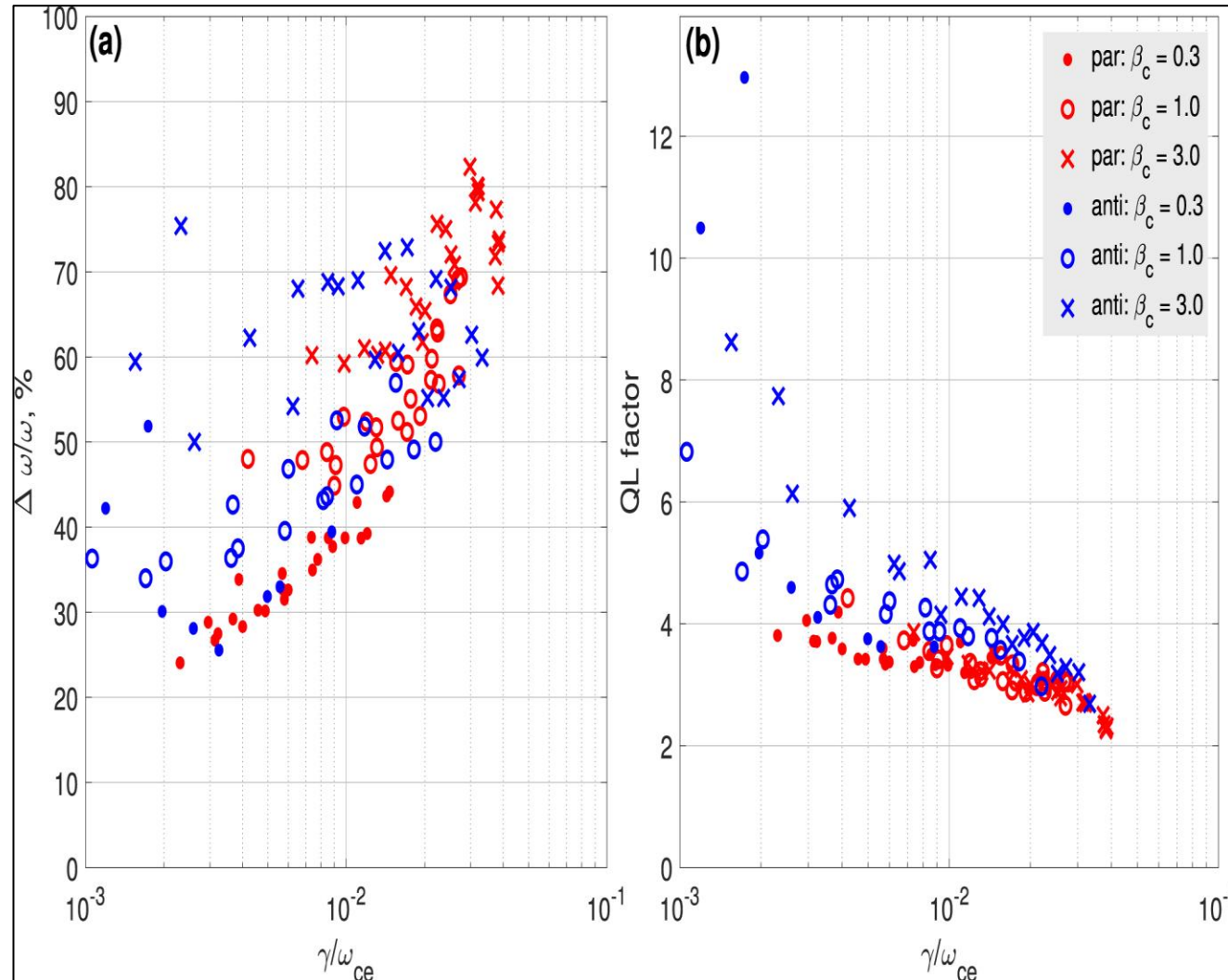
Wave frequencies and spectral widths were identified via Fourier analysis.

Gaussian fitting of the signal's spectrum provided similar results in the most cases.

Quasi-linear theory applicability:

$$\frac{\Delta\omega}{\omega} \gg \left(\frac{B_w}{B_0}\right)^{1/2} \left(\frac{\beta\omega}{\omega_{ce} - \omega}\right)^{1/4}$$

Karpman, SSRv, 1974; Tong et al., ApJ, 2019



Summary

- We modeled generation of whistler waves driven by the combined heat flux and anisotropy instability that likely operates in the solar wind.
- We found a positive correlation between linear increment and saturated wave amplitude and investigated the corresponding relation for different plasma parameters. It has been shown that a simple relation $B_w = C\gamma_{lin}^\nu$ exists, with $\nu \in (0.6, 0.9)$
- Our calculations suggest that whistler waves generated by the combined heat flux + anisotropy instability can contribute to the heat flux regulation.
- Spectral analysis of the generated whistler waves demonstrate that the quasi-linear theory should be applicable, as the frequency spectrum is sufficiently wide.

1. I Kuzichev, I Vasko, A Artemyev, SD Bale, F Mozzer (2023), Particle-In-Cell Simulations of Sunward and Anti-sunward Whistler Waves in the Solar Wind, *The Astrophysical Journal*, 959 65 DOI 10.3847/1538-4357/acfd28

2. Vasko, I. Y., I. V. Kuzichev, A. V. Artemyev, S. D. Bale, J. W. Bonnell, and F. S. Mozer (2020), On quasi-parallel whistler waves in the solar wind, *Physics of Plasmas* 27, 082902; <https://doi.org/10.1063/5.0003401>

3. Kuzichev I.V., I. Yu. Vasko, A.R. Soto-Chavez, Y. Tong, A. V. Artemyev, S.D. Bale, and A. Spitkovsky, (2019), Nonlinear Evolution of the Whistler Heat Flux Instability, *ApJ* 882 81, doi: 10.3847/1538-4357/ab3290

Thank you!