

Continuous Gravitational Waves and Neutron stars Workshop  
MPI, Hannover, 17- 20 June, 2024

R-modes as probe of Dark matter in neutron stars

(S. Shirke, S. Ghosh et al, Journal of Cosmology and Astroparticle Physics(JCAP) 12 (2023), 008)

Suprovo Ghosh

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Collaborators :

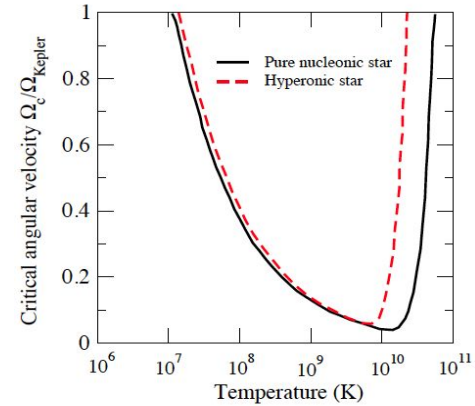
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Dr. Laura Sagunski, Prof. J. Schaffner-Bielich (ITP Frankfurt)



## R-modes as source of CGW

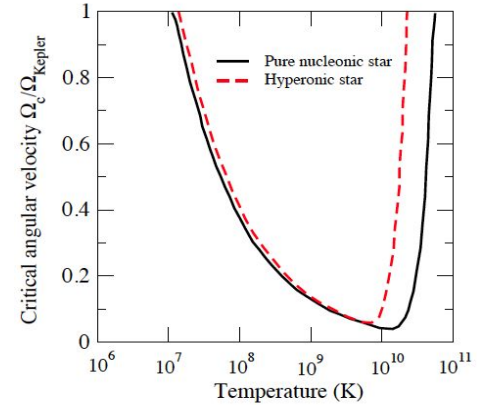
- Toroidal mode of fluid oscillation in neutron stars for which the restoring force is the Coriolis force.
- Unstable in all rotating stars due to the Chandrasekhar- Friedman -Schutz(CFS) mechanism although dissipation mechanisms can damp and saturate the oscillations. Dissipation timescales determine the instability window.
- Spindown of young pulsars, accreting pulsars leading to continuous GW emissions.



**R-mode instability window  
(Chatterjee+ 2006)**

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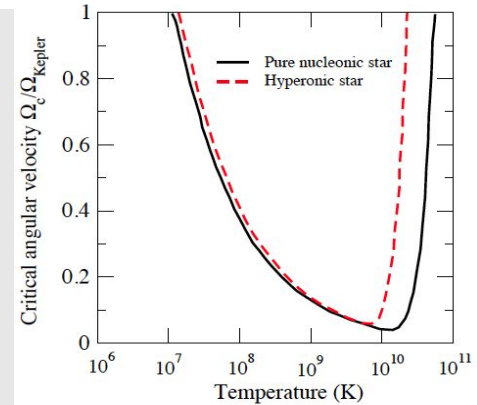
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- EOS inference from r-modes - **Ghosh, MNRAS 525, 448-454 (2023)**



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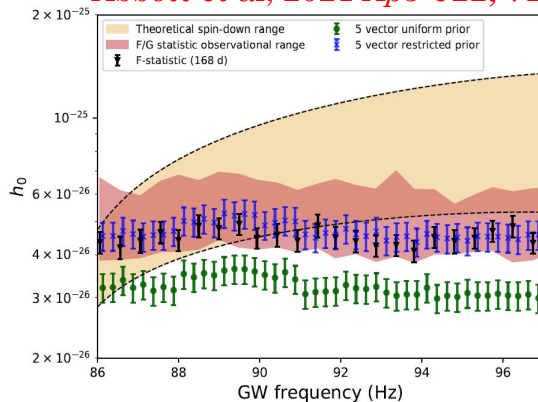
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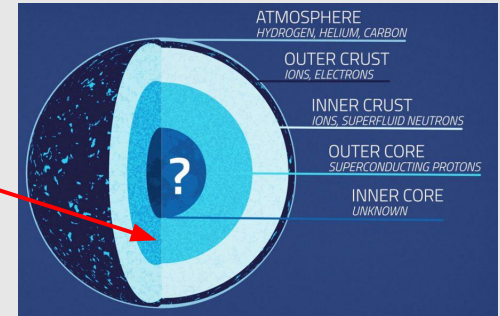
Abbott et al, 2021 *ApJ* 922, 71



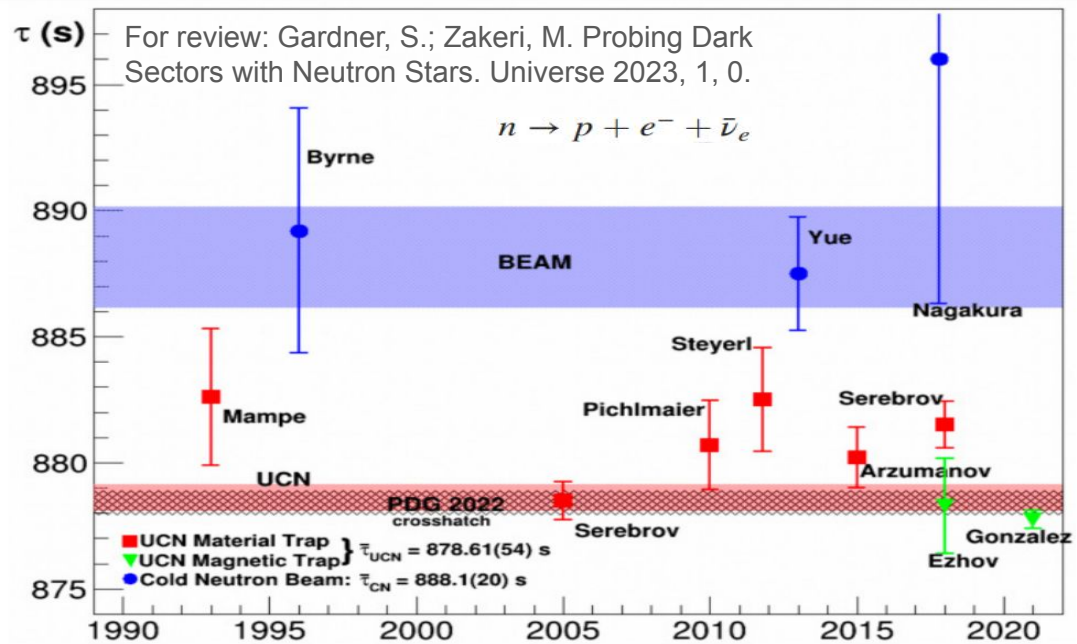
- GW Searches using LVK data :
  - Crab pulsar (Rajbhandari et al. 2021)
  - PSR J0537-6910 with  $n \approx 7$  (Fesik & Papa 2020, Abbott et al. 2021)
- No detection of GW but upper limits on r-mode amplitude were obtained.

# Dark matter in Neutron stars

- Dark matter  $\sim 25\%$  of the Universe.
- Particle nature of dark matter still unknown.
- Possibility of Dark matter-admixed neutron star with a DM core or a DM halo.
- Primary driving mechanisms:
  - Accretion/Capture
  - Particle Decay
  - DM Seed
- Constraints on the dark matter mass and self-interaction from neutron star observations.

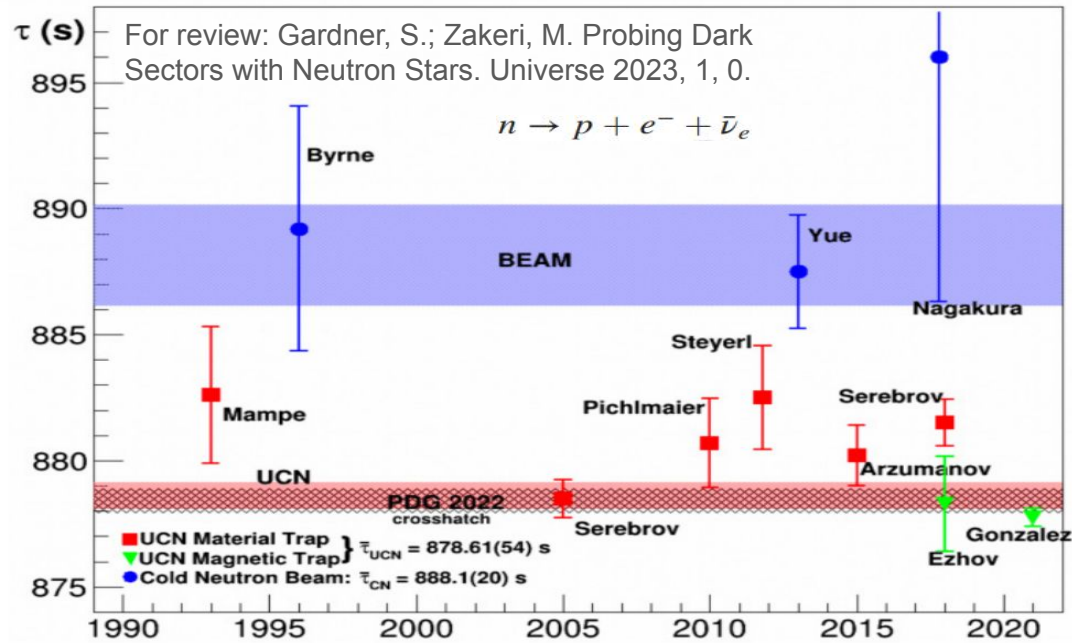


# Neutron Decay Anomaly



- Neutron lifetime:
  - Bottle/Trap Method
  - Beam Method
- Discrepancy in measured lifetime:  
 $\Delta\tau \sim 9.5$  s with  $4\sigma$
- Dark decay channel?
- Branching ratio  $\sim 1\%$   
i. e.  $\Gamma_{\text{dark}}/\Gamma_{\text{proton}} \approx 1/100$

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PHYSICAL REVIEW LETTERS **120**, 191801 (2018)

Editors' Suggestion

Featured in Physics

Possibility of a dark decay Channel ?

$$n \rightarrow \chi + \phi$$

## Dark Matter Interpretation of the Neutron Decay Anomaly

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# EOS model description

- Hadronic Matter: Relativistic Mean-Field Model (RMF)

$$\mathcal{L}_{int} = \sum_N \bar{\psi}_N \left[ g_\sigma \sigma - g_\omega \gamma^\mu \omega_\mu - \frac{g_\rho}{2} \gamma^\mu \boldsymbol{\tau} \cdot \boldsymbol{\rho}_\mu \right] \psi_N - \frac{1}{3} b n_N (g_\sigma \sigma)^3 - \frac{1}{4} c (g_\sigma \sigma)^4$$

$$+ \Lambda_\omega (g_\rho^2 \boldsymbol{\rho}^\mu \cdot \boldsymbol{\rho}_\mu) (g_\omega^2 \omega^\nu \omega_\nu) + \frac{\zeta}{4!} (g_\omega^2 \omega^\mu \omega_\mu)^2$$

Parameters:

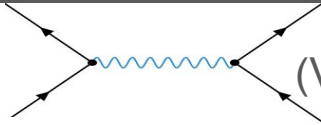
$\{n_{sat}, E_{sat}, K_{sat}, E_{sym}, L_{sym}, m^*/m\}$

| Model        | $n_{sat}$<br>(fm <sup>-3</sup> ) | $E_{sat}$<br>(MeV) | $K_{sat}$<br>(MeV) | $E_{sym}$<br>(MeV) | $L_{sym}$<br>(MeV) | $m^*/m$ |
|--------------|----------------------------------|--------------------|--------------------|--------------------|--------------------|---------|
| HTZCS [86]   | 0.15                             | -16.0              | 240                | 31                 | 50                 | 0.65    |
| Stiffest [7] | 0.145                            | -15.966            | 238.074            | 31.080             | 56.483             | 0.550   |

[86] Hornick et al., PRC 98 (2018) [7] Ghosh, D. C., Schaffner-Bielich, EPJA 58 (2022)

- Dark Matter: Self-interacting fermionic DM in chemical equilibrium

$n \rightarrow \chi + \phi$



(Vector repulsion)  $\mu_\chi = \mu_n$

$$\mathcal{L} \supset -g_V \bar{\chi} \gamma^\mu \chi V_\mu - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu$$

$$\mu_\chi = \sqrt{k_{F\chi}^2 + m_\chi^2} + G n_\chi$$

$$\epsilon_{DM} = \frac{1}{\pi^2} \int_0^{k_{F\chi}} k^2 \sqrt{k^2 + m_\chi^2} dk + \frac{1}{2} G n_\chi^2$$

938 MeV =

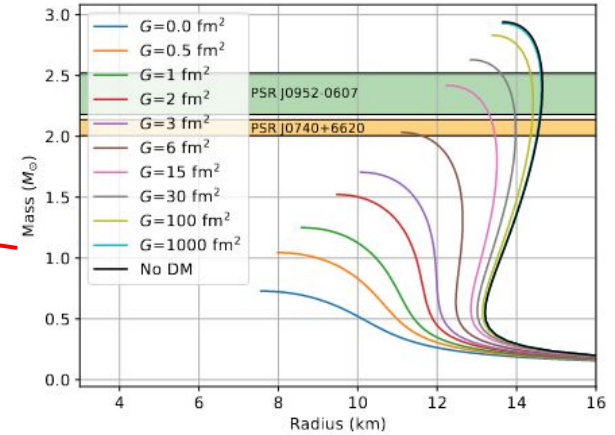
$$G = \left( \frac{g_V}{m_V} \right)^2 \quad n_\chi = \frac{k_{F\chi}^3}{3\pi^2}$$



# Cross Section and Shear Viscosity

- Constraints on the self-interaction strength( $G$ ) from multi-messenger observations.

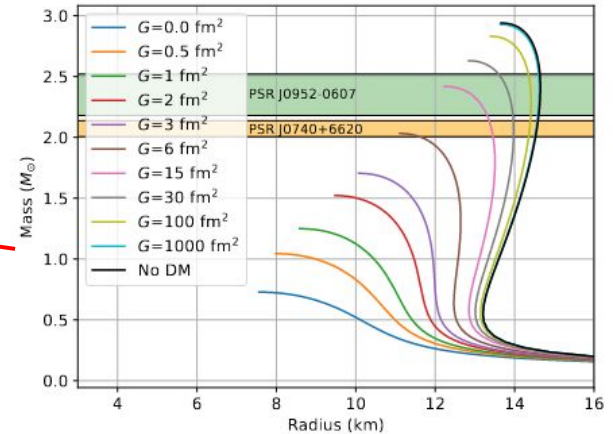
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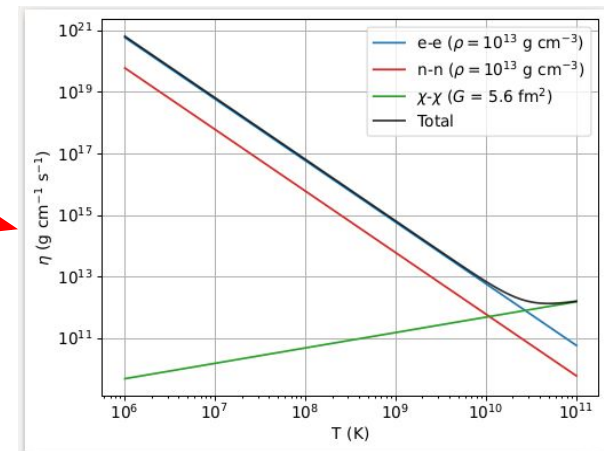
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- Shear viscosity from the kinetic theory -

$$\eta_{\chi} \approx \frac{\sqrt{m_{\chi} k T}}{\sigma_{\chi}}$$

- Negligible compared to the canonical shear viscosity .
- Ongoing microscopic calculation for shear viscosity from DM.(Shirke et al., To be published)



# Bulk viscosity and the reaction timescale

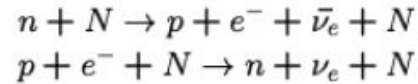
- Bulk viscosity depends on the relaxation timescale of the reaction.

$$\zeta = P(\gamma_\infty - \gamma_0) \frac{\tau}{1 + (\omega\tau)^2}$$

Experimental constraints :  $\Gamma_{\text{dark}}/\Gamma_{\text{proton}} \approx 1/100$

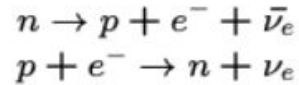
Dark sector Process:  $n \leftrightarrow \chi + \varphi$

1. Modified URCA  
Process :

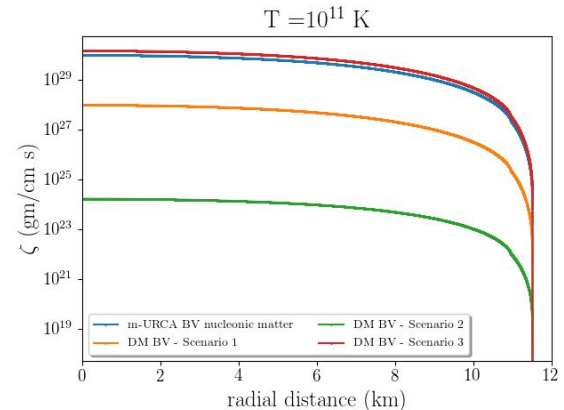
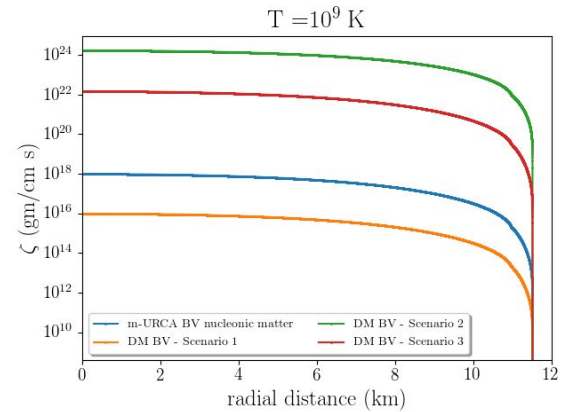


2. Constant timescale :  $\tau = 8.88 \times 10^4 \text{ sec}$

3. Direct URCA process:



- Two free parameters:  $G$  and  $\tau$
- Negligible effect of  $G$

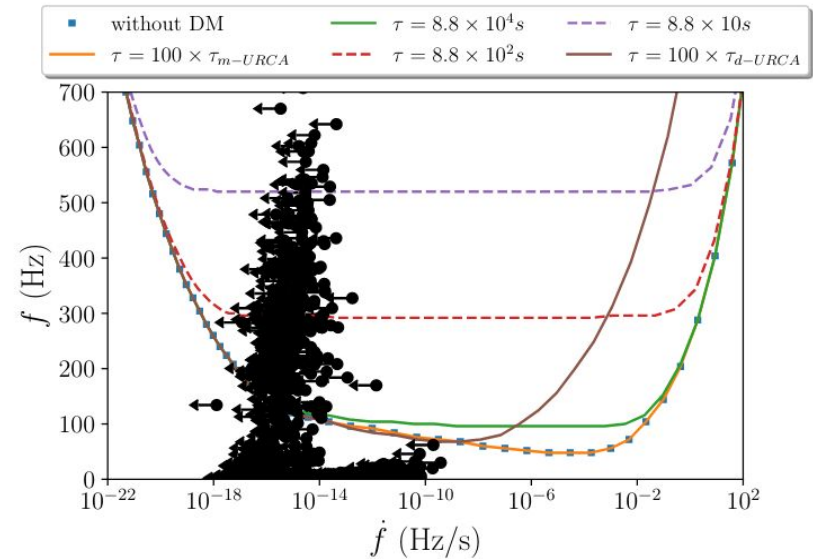
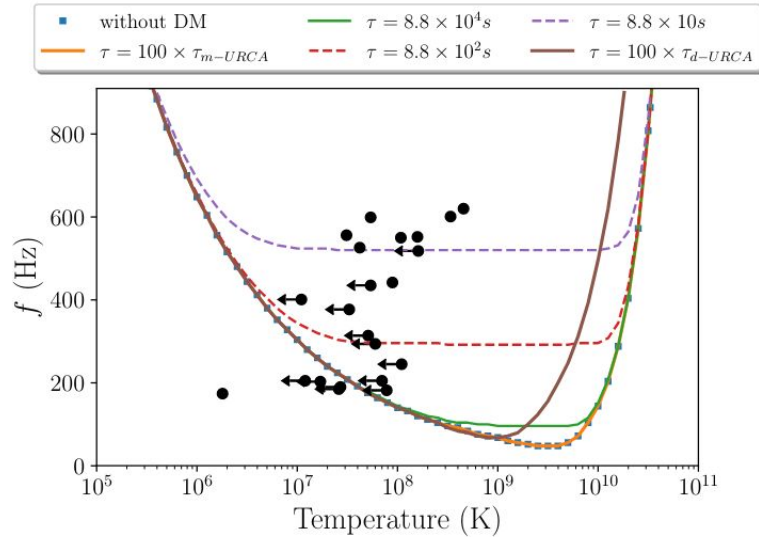


# R-mode instability window

- Boundary obtained by matching the dissipation and GW emission timescales.

$$\frac{1}{\tau(\Omega_c)} = \frac{1}{\tau_{GW}(\Omega_c, T)} + \frac{1}{\tau_{SV}(\Omega_c, T)} + \frac{1}{\tau_{BV}(\Omega_c, T)} = 0$$

- $f$ - $T \rightarrow f$ - $\dot{f}$  boundary - assuming that the power-loss due to the spin-down driven by r-mode instability is equal to the luminosity (both neutrino and photon luminosity) of the star.



## Summary

- **First investigation of the effect of DM on r-modes of NSs and instability window**
- **Hadronic model: RMF; DM model: Neutron Decay Anomaly**
- **Constraints: CEFT, Multi-messenger astrophysics**
- **$G > 5.6 \text{ fm}^2$  &  $f_{\text{DM}} < 37.9\%$ ;  $f_{\text{DM}} < 13.7\%$  for  $\sigma/m > 0.1 \text{ cm}^2/\text{g}$**

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- **Shear Viscosity from DM-DM scattering using Kinetic Theory**
- **DM SV negligible for  $T < 10^{10} \text{ K}$**
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- **DM BV significant in cases when  $\tau_{\text{DM}} = 100 \times \tau_{\text{d-Urca}}$  and  $\tau = \text{constant}$**
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- **Future: Possible for any other DM model?  
Microscopic calculation for SV?**